



# KYNrefrev – reflection reverberation model

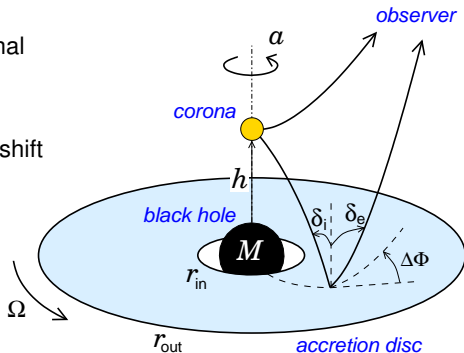
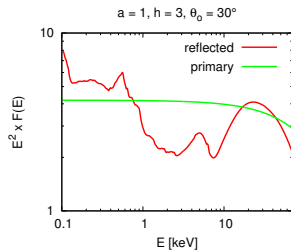
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*The X-ray Spectral-Timing Revolution*  
Lorentz Center, Leiden, Netherlands  
1<sup>st</sup> – 5<sup>th</sup> February 2016

# Scheme of the lamp-post geometry

- ▶ **central black hole** – mass, spin
- ▶ **compact corona** with isotropic emission  
→ height, photon index
- ▶ **accretion disc**  
→ Keplerian, geometrically thin, optically thick  
→ ionisation due to illumination  
( $L_p$ ,  $h$ ,  $M$ ,  $a$ ,  $n_H$ ,  $q_n$ )
- ▶ **local re-processing** in the disc  
→ REFLIONX with different directional emissivity prescriptions
- ▶ **relativistic effects**:  
→ Doppler and gravitational energy shift  
→ light bending (lensing)  
→ aberration (beaming)  
→ light travel time
- ▶ **KYNrefrev**



# KYNrefrev parameters

1	a/M	GM/c	1.00000
2	theta_o	deg	30.0000
3	rin	GM/c^2	1.00000
4	ms		1
5	rout	GM/c^2	1000.00
6	phi	deg	0.0
7	dphi	deg	360.000
8	M/M8		0.100000
9	height	GM/c^2	3.00000
10	PhoIndex		2.00000
11	L/Ledd		1.00000E-03
12	Np:Nr		1.00000
13	density		1.00000
14	den_prof		0.0
15	abun		1.00000
16	alpha	GM/c^2	-6.00000
17	beta	GM/c^2	0.0
18	rcloud	GM/c^2	0.0
19	zshift		0.0
20	limb		0.0
21	tab		2
22	sw		2
23	duration	GM/c^3	10.0000
24	deltaT	GM/c^3	1.00000
25	nt		256.000
26	ntable		80.0000
27	nrad		500.000
28	division		-1.00000
29	nphi		180.000
30	nt_ratio		1.00000
31	time	sec/Rg	0.0
32	xsw		0
33	smooth		1.00000
34	nthreads		4.00000
35	norm		1.00000

## Parameters describing:

- ▶ physical properties of the system (blue)
- ▶ reflection area and absorption by cloud (green)
- ▶ resolution in time, radius and azimuth (red),  
→ affect speed of the code,  
→ defaults should be OK, except for extreme cases of low height and low or high inclination
- ▶ output inside xspec (orange)

## KYNrefrev output

- ▶ spectrum integrated over time
- ▶ time evolving spectrum of the reflection
- ▶ light curves for different energy bands
- ▶ real and imaginary parts, amplitudes and phases for both relative reflection and total signal both for each energy bin and energy band
- ▶ real and imaginary parts, amplitudes and phases and time delay integrated in frequency range up to the first zero point

# Recent developments and future plans

## Recent updates:

- ▶ re-write into C and as XSPEC model with sum speed-ups
- ▶ further speeding up by optimizing resolution parameters

## Future plans:

- ▶ near future: extrapolation of tail and break due to outer radius
- ▶ more physical prescription of disc density (Novikov-Thorne)
- ▶ models for neutral cold disc (Goosmann+NOAR), XILLVER and REFHIDEN
- ▶ more distant future: off-axis flares and extended corona

# Transfer function for reverberation

Response to the on-axis primary emission:

$$F(E, t) = \int dt' \int dS G(r, \varphi) \times \\ N_p(t') N_{\text{inc}}(r) M(r, \varphi, E/g, t' + t_{\text{pd}}) \delta([t - t_{\text{do}}] - [t' + t_{\text{pd}}])$$

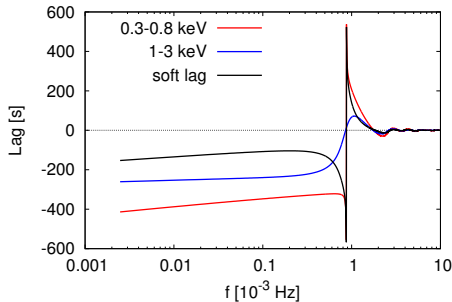
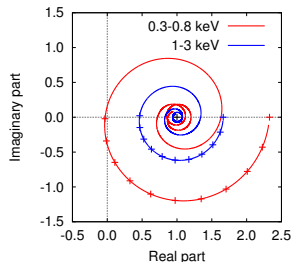
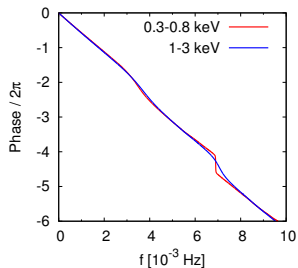
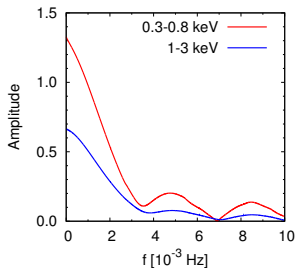
Transfer function  $\psi(E, t) \rightarrow$  response to a flare [ $N_p(t') = \delta(t')$ ]:

$$F(E, t) = \int dt' N_p(t') \psi(E, t - t')$$

$$\hat{\psi}_r(E, f) = A_r(E, f) e^{i\phi_r(E, f)} \quad \psi_r(E, t) = \frac{F_r(E, t)}{F_p(E)}$$

$$\tau(E, f) = \frac{1}{2\pi f} \text{atan} \frac{A_r(E, f) \sin \phi_r(E, f)}{1 + A_r(E, f) \cos \phi_r(E, f)}$$

# Fourier transform

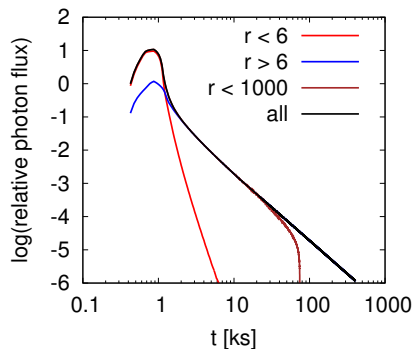


$$a = 1, \theta_0 = 30^\circ, h = 3, \Gamma = 2,$$

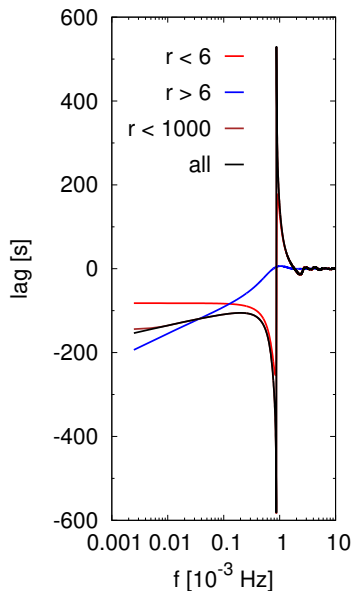
$$L_{X,\text{obs}}(2 - 10\text{keV}) = 0.001 L_{\text{Edd}},$$

$$M = 10^7 M_\odot, n_{\text{H}} = 10^{15} \text{cm}^{-3}, q_n = 0$$

## Tail – inner and outer echo

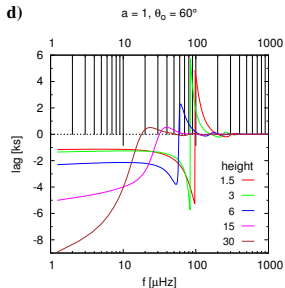
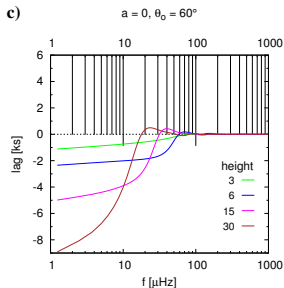
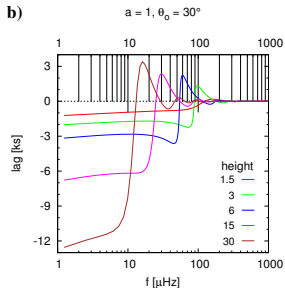
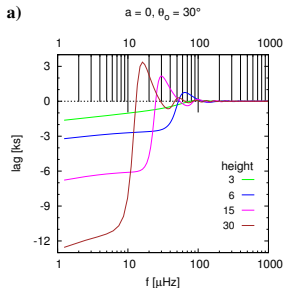


- ▶ outer tail in Newton with perfect disc reflection:  $\sim t^{-2}$
- ▶ radial ionisation dependence may change the tail index:  $\sim t^{-q}$
- ▶ different contributions of inner and outer parts at low and high frequencies





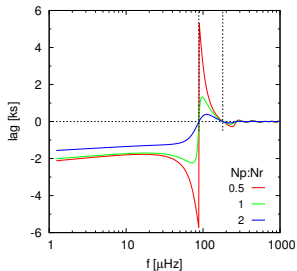
# Lag dependence on geometry



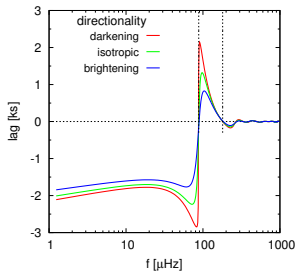
- ▶ the lag amplitude:
  - ▶ the lag increases with height
  - ▶ the lag decreases with inclination (exception: low heights and high spin)
  - ▶ the lag decreases with spin (exception: low heights and high inclination)
- ▶ the lag null points (due to phase wrapping)
  - ▶ shift to lower frequencies for higher heights due to longer timescales of response
  - ▶ change slightly with the inclination
  - ▶ change negligibly with the spin

# Lag dependence on other parameters

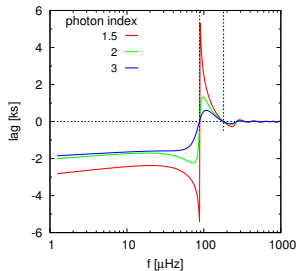
a) Dependence on primary emission directionality



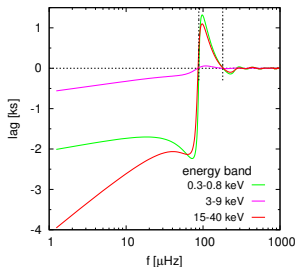
b) Dependence on reflection directionality



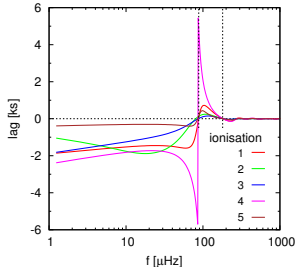
c) Dependence on photon index



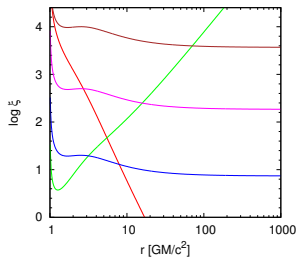
d) Dependence on energy band



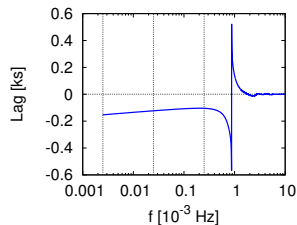
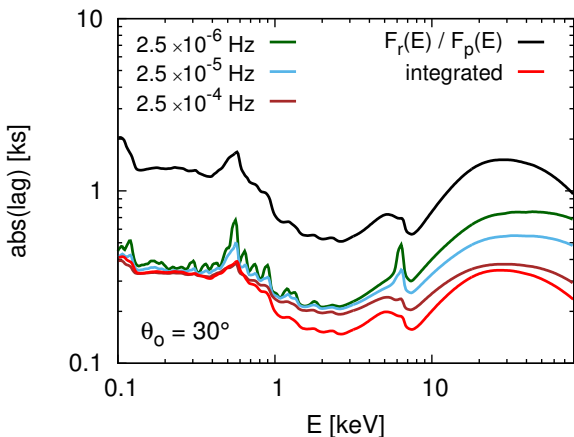
e) Dependence on disc ionisation



f) Disc ionisation profile



# Lag energy dependence



- ▶ lag–energy dependence follows the relative reflection spectrum
- ▶ flattening due to  $\arctan$  and division by  $(1 + A_r \cos \phi_r)$
- ▶ low/high frequencies have less/more diluted spectra due to reflection from outer/inner disc regions